

**Note: Show all your work. No credits for answers not supported by work.**

**Problem 1:** (30 points) Find each of the following limits if it exists.

(a)  $\lim_{x \rightarrow 3} \frac{x^2 - x - 6}{x^2 - 9}$

(b)  $\lim_{x \rightarrow 0^+} \frac{x}{\sqrt{x^2 + 4} - 2}$

(c)  $\lim_{x \rightarrow \infty} \frac{3x^2 + 4x - 9}{1 + 3x - 2x^2}$

**Problem 2:** (20 points)

(a) Find all vertical and horizontal asymptotes of  $y = \frac{x}{2x^2 - x}$ .

(b) Find all values of A and B which will make the function continuous at  $x = 2$ .

$$f(x) = \begin{cases} \sqrt{1-x} & \text{if } x < 1 \\ A & \text{if } x = 1 \\ 2x + B(x+1) & \text{if } x > 1. \end{cases}$$

**Problem 3:** (20 points)

(a) Use the definition of the derivative to find  $f'(2)$  for the function  $f(x) = 2x^2$ .

(b) The cost function of producing  $x$  units is  $C(x) = x^3 - 6x^2 + 15x$

(i) Find the marginal cost function.

(ii) Estimate the cost of producing the unit number 11. (Do not find the exact cost)

**Problem 4:** (30 points)

(a) If  $y = (x+1)^x$ , find  $y'(1)$ .

(b) Find the slope of the line tangent to the graph of  $y + xe^y = 1$  at the point  $(1, 0)$ .

(c) Find  $\frac{d^2y}{dx^2}$  for the function  $y = 2^{3x} - \ln x$