

**King Fahd University of Petroleum and Minerals**  
 Department of Mathematical Sciences  
 MATH 201- Calculus-III (041)  
 Major Examination I (Sections 8 and 11)  
 October 16,2004

Time: 90 Minutes

Grade: 60

Instructor : Dr. Abdul Rahim Khan

**SHOW COMPLETE AND NEAT WORK FOR FULL CREDIT.**

1. Find area of:
  - (i) one loop of the graph of  $r=3\cos 5\theta$ .
  - (ii) the region inside the circle  $r = 1$  and outside the cardioid  
 $r = 1 - \cos \theta$ . (5+5)
2. On the cardioid  $r=1+\sin\theta$ , find points where tangent line is vertical. (5)
3. Include all details to sketch the graph of  $r^2=4\cos\theta$  (5)
4. Calculate area of the surface generated by revolving the graph of  $r^2 = 2\cos 2\theta$  about the polar axis where  $0 \leq \theta \leq \pi$ . (10)
5. (i) Two spheres  $S_1$  and  $S_2$  are centered at the origin and are tangent to the sphere of radius 1 centered at  $(5,-2,3)$ . Write equations of  $S_1$  and  $S_2$ .  
 (ii) Find 2 unit vectors that are perpendicular to the line  $y=-3x+1$ . (5+5)
6. (i) Do the vectors

$$\vec{U} = \langle 1, -2, 1 \rangle$$

$$\vec{V} = \langle 3, 0, -2 \rangle$$

$$\vec{W} = \langle 5, -4, 0 \rangle$$

lie in the same plane ? Justify.

(ii) Show that  $\|\vec{U} \times \vec{V}\|^2 = \|\vec{U}\|^2 \|\vec{V}\|^2 - (\vec{U} \cdot \vec{V})^2$  (5+5)

7. Check whether the lines are parallel or skew lines:

$$\begin{aligned} L_1 : & \quad x = 1 + t, \quad y = -2 + 3t, \quad z = 4 - t \\ L_2 : & \quad x = 2t, \quad y = 3 + t, \quad z = -3 + 4t \end{aligned} \quad (5)$$

8 Find the distance between lines.

$$\begin{aligned} L_1 : & \quad x = 2t, \quad y = 3 + 4t, \quad z = 2 - 6t \\ L_2 : & \quad x = 1 + 3t, \quad y = 6t, \quad z = -9t \end{aligned} \quad (5)$$