

King Fahd University of Petroleum and Minerals
 Department of Mathematical Sciences
 MATH 201- Calculus-III (041)
 Major Examination II (Sections 8 and 11)
 December 4,2004

Time: 90 Minutes

Grade: 60

Instructor : Dr. Abdul Rahim Khan

SHOW COMPLETE AND NEAT WORK FOR FULL CREDIT.

1. (i) Find equation of a plane whose points are equidistant from the points (4,-2,2) and (3,2,5).
 (ii) Find point of intersection of the plane $2x + 3y - z = 0$ and the line through (2,1,0) that is perpendicular to the plane.

(5+5)

2. (i) Identify and sketch the surface obtained by revolving the graph of $z^2 - x^2 = 1$ about the x -axis.
 (ii) Describe curve of intersection between the surfaces $z = x^2 + y^2$ and $z = 8 - x^2 - y^2$.

(5+5)

3. Evaluate $\lim_{(x,y) \rightarrow (0,0)} \left[\frac{x^2 - y^2}{\sqrt{x^2 + y^2}} + \frac{\sin h(4x^2 + 4y^2)}{x^2 + y^2} \right]$ (5)

4. (i) Sketch the level surface for $f(x, y, z) = z - (x + 3)^2 - (y - 2)^2 + 16$ when $k=8$.

(ii) $f(x, y) = \begin{cases} \frac{2x^2y}{x^4 + y^2} & (x, y) \neq (0, 0) \\ 0 & (x, y) = (0, 0) \end{cases}$

Check whether or not f is continuous at (0,0). (5+5)

5. Suppose that $\ln(2x^2 + y - z^3 + 3w) = z$. use implicate differentiation to find $\frac{\partial w}{\partial z}$.

(5)

6. The function $f(x, y) = x^2y$ has a local linear approximation $L(x, y) = 4y - 4x + 8$ at a point $P_0(x_0, y_0)$. Find the point P_0 .

(5)

7. Define $f : \mathbb{R}^2 \rightarrow \mathbb{R}$ by

$$f(x, y) = \begin{cases} \frac{xy(x^2 - y^2)}{x^2 + y^2} & (x, y) \neq (0, 0) \\ 0 & (x, y) = (0, 0) \end{cases}$$

Show that $f_{xy}(0, 0) \neq f_{yx}(0, 0)$.

(10)

8. Let $w = r^2 + sv + t^3$ where

$$r = x^2 + y^2 + z^2, s = xyz, v = xe^y \text{ and } t = yz^2.$$

Use chain rule to calculate $\frac{\partial w}{\partial z}$.

(5)