

King Fahd University of Petroleum and Minerals  
College of Sciences  
Quiz #6(A)

St. ID:

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Q1: Suppose that 8% of the items produced by a certain company is defective. A random sample of 10 items has been selected from the product of this company. Then find:

a) the probability that the sample contains at least 2 defective items.

**Solution:** Let  $X$  = the number of defective items in the sample. Then

$$X \sim b(10, 0.08) \text{ and } f(x) = \binom{10}{x} (.08)^x (.92)^{(10-x)}, x = 0, 1, \dots, 10.$$

$$\begin{aligned} \text{Then } P(\text{that the sample contains at least 2 defective items}) &= P(X \geq 2) \\ &= 1 - P(X \leq 1) = 1 - f(0) - f(1) = 1 - (0.92)^{(10)} - 10(.08)(0.92)^{(9)} \end{aligned}$$

b) the probability that the sample contains at most 2 defective items given that the sample contains between 1 and 4 defective items .

**Solution:**  $P(\text{that the sample contains at most 2 defective items given that the sample contains between 1 and 4 defective items}) = P(X \leq 2 / 1 \leq X \leq 4)$

$$= P(X \leq 2, 1 \leq X \leq 4) / P(1 \leq X \leq 4) = P(1 \leq X \leq 2) / P(1 \leq X \leq 4)$$

$$= (f(1) + f(2)) / (f(1) + f(2) + f(3) + f(4))$$

$$\begin{aligned} &= \frac{(10(.08)(0.92)^{(9)} + 10C2(.08)^2(0.92)^{(8)})}{(10(.08)(0.92)^{(9)} + 10C2(.08)^2(0.92)^{(8)} + 10C3(.08)^3(0.92)^{(7)} + 10C4(.08)^4(0.92)^{(6)}} \end{aligned}$$

c) What is the expected number of defective items in the sample?

**Solution:** The expected number of defective items in the sample =  $E(X)$   
 $= (10)(0.08) = 0.8$

Q2: Let  $Z$  has a standard normal distribution. Then find:

a)  $P(-0.75 \leq Z \leq 1.05)$

**Solution:**  $P(-0.75 \leq Z \leq 1.05) = A(1.05) + A(0.75)$

$$= 0.3531 + 0.2734 = 0.6265$$

b) a such that  $P(a \leq Z) = 0.93$

**Solution:**  $P(a \leq Z) = 0.93$  implies that :  $A(a) + 0.5 = 0.93$ . Then  $A(a) = 0.43$   
 Which implies that  $a = -1.48$