

**Show all your work. No credits for answers not supported by work.**

1. A rectangular *closed* box with a square base is to have a volume of  $1000 \text{ in}^3$ . Find its dimensions if the box is to require the least amount of material.
2. Use differentials to approximate  $\sqrt{25.6}$
3. If the marginal revenue for a manufacturer's product is  $\frac{dR}{dq} = 700 - 6q - 8q^3$ , find the demand equation.
4. Find the area enclosed by the graphs of  $y = x^2 - 5$  and  $y = 2x + 3$ .
5. Evaluate the integrals:
  - a.  $\int x(1 - 2x^2)^5 dx$
  - b.  $\int \frac{3x + 2}{x - 1} dx$
  - c.  $\int e^{2\ln(x-3)} dx$
  - d.  $\int (1 + 3^x)^2 dx$

**Show all your work. No credits for answers not supported by work.**

1. A rectangular *open* box with a square base is to have a volume of  $500 \text{ in}^3$ . Find its dimensions if the box is to require the least amount of material.
2. Use differentials to approximate  $\ln(1.03)$
3. If the marginal revenue for a manufacturer's product is  $\frac{dR}{dq} = 500 - 12q^2 - 8q^3$ , find the demand equation.
4. Find the area enclosed by the graphs of  $y = x^2 - 5$  and  $y = 3 - 2x$ .
5. Evaluate the integrals:
  - a.  $\int x^2(1 - 2x^3)^4 dx$
  - b.  $\int \frac{2x - 1}{x + 2} dx$
  - c.  $\int \frac{x + x \ln x}{x^2} dx$
  - d.  $\int \frac{1 + 2^x}{5^x} dx$