

Problem 1: (15 points) If it exists, find the limit. Use the symbols ∞ or $-\infty$ as appropriate.

a) $\lim_{x \rightarrow 1^-} \frac{|x^2 - x|}{x - 1}$

b) $\lim_{x \rightarrow 3^+} \ln(x - 3)$

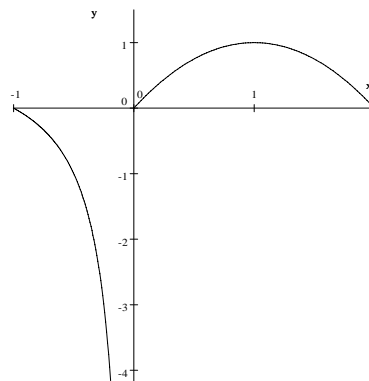
c) $\lim_{y \rightarrow 0} \frac{4y + y^2}{3y - y^2}$

d) $\lim_{x \rightarrow 5^+} (x - \llbracket x \rrbracket)$

e) $\lim_{x \rightarrow 0} \frac{\sqrt{x^2 + 9} - 3}{x^2}$

Problem 2: (5 points) consider the graph of the function $f(x)$ whose graph is sketched below. Determine whether each of the following statements is true or false (CIRCLE ONE).

- | | | |
|---|---|---|
| a. $\lim_{x \rightarrow 1} f(x) = 1$ | T | F |
| b. $\lim_{x \rightarrow 1} f(x) = f(1)$ | T | F |
| c. $\lim_{x \rightarrow 0} f(x)$ does not exist. | T | F |
| d. $\lim_{x \rightarrow 1} \frac{f(x)}{x - 1} = \infty$ | T | F |
| e. $f(x)$ has a vertical asymptote | T | F |



Problem 3: (5 points) Use the $\epsilon - \delta$ definition of the limit to show that $\lim_{x \rightarrow 2} (1 - 2x) = -3$.

Problem 1: (15 points) If it exists, find the limit. Use the symbols ∞ or $-\infty$ as appropriate.

a) $\lim_{x \rightarrow 1^+} \frac{|x^2 - x|}{x - 1}$

b) $\lim_{x \rightarrow 2^-} \ln(2 - x)$

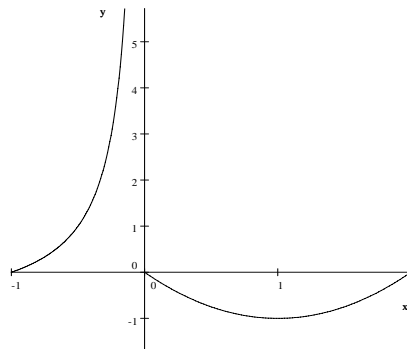
c) $\lim_{y \rightarrow 0} \frac{5y + y^2}{3y - y^2}$

d) $\lim_{x \rightarrow 4^+} (x - \lceil x \rceil)$

e) $\lim_{x \rightarrow 1} \frac{\sqrt{x + 3} - 2}{x - 1}$

Problem 2: (5 points) consider the graph of the function $f(x)$ whose graph is sketched below. Determine whether each of the following statements is true or false (CIRCLE ONE).

- | | | |
|--|---|---|
| a. $\lim_{x \rightarrow 1} f(x) = -1$ | T | F |
| b. $\lim_{x \rightarrow 1} f(x) = f(1)$ | T | F |
| c. $\lim_{x \rightarrow 0} f(x)$ does not exist. | T | F |
| d. $\lim_{x \rightarrow 1} \frac{f(x)}{x - 1} = -\infty$ | T | F |
| e. $f(x)$ has a vertical asymptote | T | F |



Problem 3: (5 points) Use the $\epsilon - \delta$ definition of the limit to show that $\lim_{x \rightarrow 2} (2 - 3x) = -4$.