

Q1- Find the Laplace transform of the following functions:

a-  $f(t) = \cos^2(t)$

b-  $f(t) = e^{-2t} \cos(4t)$

c-  $f(t) = t \sinh t$ .

d-  $f(t) = 1 * t^3$

e-  $f(t) = \begin{cases} \sin(t), & 0 \leq t \leq \pi \\ 0, & t \geq \pi. \end{cases}$

Q2- Find the inverse transform of the functions:

a-  $\mathcal{L}^{-1} \left\{ \frac{4s}{4s^2+1} \right\}$

b-  $\mathcal{L}^{-1} \left\{ \frac{s}{s^2+2s-3} \right\}$

Q3- Use Laplace transform to solve the initial value problem:  $y'' - 4y' + 4y = t^3 e^{2t}$ ,  $y(0) = 0, y'(0) = 0$ .