

**Show all your work. No credits for answers not supported by work**

1. Find the power series representation of  $\frac{1}{1+x}$

2. Use (1) above to find the Maclaurin series representation of  $\frac{t}{1+t^2}$

3. Find the Maclaurin series representation of  $\ln(1+x^2)$ .

Note: you may use  $\int_0^x \frac{t}{1+t^2} dt$ .

4. What is the radius of convergence of the power series in (4)

5. Use (4) to find the sum of the alternating **harmonic series**  $\sum_{n=1}^{\infty} \frac{(-1)^{n+1}}{n}$

6. Find the Taylor series of  $\frac{1}{1+x}$  centered at  $c = 2$  (i. e. in powers of  $(x-2)$ )