

Name: _____

								<i>Math – 132</i>	<i>Term – 093</i>	<i>Section 01</i>
								<i>SUMTW</i>	<i>10 : 30 am</i>	<i>11 : 30 am</i>
<i>CODE</i>	<i>CODE</i>	<i>CODE</i>	<i>CODE</i>	<i>MARKS : 126</i>	<i>SERIAL</i>					
001*	002	003	004	<i>Time : 2Hours</i>	<i>Number</i>					

- NOTE: 1. The questions are not in any order of difficulty at all.
2. All questions carry equal number of marks.
 3. Only the nonprogrammable calculators are allowed.
 4. All types of PAGERS, OR MOBILES ARE NOT ALLOWED to be with you during the examination.
 5. Use an HB 2 pencil.
 6. Use a good eraser. Do not use the eraser attached to the pencil.
 7. Write your name, ID number and Section number on the examination paper and in the upper left corner of the answer sheet.
 8. When bubbling your ID number and Section number, be sure that bubbles match with the number that you write.
 9. The test Code Number is already typed and bubbled in your answer sheet. Make sure that it is the same as that printed on your question paper.
 10. When bubbling, make sure that the bubbled space is fully covered.
 11. When erasing a bubble, make sure that you do not leave any trace of penciling.
 12. Count that the Examination has TWENTY-ONE Questions and TWELVE Pages.
 13. Please BUBBLE carefully only right answer letter (*A* or *B* or *C* or *D* or *E*) corresponding to the correct answer to each question in the enclosed computerized Omar Sheet, with pencil only.
 14. Please do not leave any question unbubbled in the Answer Sheet.
 15. Please check that the version of your question paper and the answer sheet enclosed with it matches correctly. The versions are Code: 001, Code: 002, Code: 003, Code: 004.

1Q1. Find the integral

$$\int \frac{x dx}{(7x^2 + 3)^5}.$$

$$(A) \longrightarrow -\frac{1}{56} (7x^2 + 3)^{-4} + C$$

$$(B) \longrightarrow -\frac{1}{14} (7x^2 + 3)^{-6} + C$$

$$(C) \longrightarrow -\frac{7}{3} (7x^2 + 3)^{-6} + C$$

$$(D) \longrightarrow -\frac{7}{3} (7x^2 + 3)^{-4} + C$$

$$(E) \longrightarrow -\frac{1}{56} \left(\frac{7}{3}x^3 + 3x \right)^{-4} + C$$

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2Q2. Find the coordinates of the points of *inflection* for the function.

$$f(x) = x^3 + 9x^2 + 24x + 18$$

$$(A) \longrightarrow (-2, -2)$$

$$(B) \longrightarrow (-4, 2)$$

$$(C) \longrightarrow (-3, 0)$$

$$(D) \longrightarrow (0, 18)$$

$$(E) \longrightarrow \text{There are no points of inflection.}$$

=====

3Q3. The function $y = 4x^3 - 10x^2 - 8x + 3$ is decreasing on

(A) $\longrightarrow \left(-\frac{1}{3}, 2\right)$

(B) $\longrightarrow \left(-\infty, -\frac{1}{3}\right)$

(C) $\longrightarrow (2, \infty)$

(D) $\longrightarrow \left(-\frac{1}{3}, \infty\right)$

(E) $\longrightarrow (-\infty, 2)$

=====

4Q4. On the interval $[0, 2]$, the function $y = 3x^4 - 4x^3$ has

(A) \longrightarrow an absolute minimum at $x = 1$ and no absolute maximum.

(B) \longrightarrow an absolute maximum at $x = 0$ and an absolute minimum at $x = 1$.

(C) \longrightarrow an absolute maximum at $x = 2$ and an absolute minimum at $x = 1$.

(D) \longrightarrow an absolute maximum at $x = 2$ and an absolute minimum at $x = 0$.

(E) \longrightarrow no absolute maximum and no absolute minimum.

=====

5Q5. If $f(x) = x^3 + 3x^2 - 24x + 8$, then f is

(A) \longrightarrow decreasing on $(-\infty, 2)$, concave up on $(-1, \infty)$, and has no relative minimum point.

(B) \longrightarrow decreasing on $(1, 2)$, concave up on $(0, \infty)$, and has a relative minimum when $x = -4$.

(C) \longrightarrow increasing on $(2, \infty)$, concave up on $(-\infty, -1)$, and has a relative minimum when $x = 2$.

(D) \longrightarrow increasing on $(-4, 2)$, concave down on $(-\infty, \infty)$, and has a relative maximum when $x = 2$.

(E) \longrightarrow decreasing on $(-4, 2)$, concave down on $(-\infty, -1)$, and has a relative maximum when $x = -4$.

=====

6Q6. The cost equation for a cookie store is given by $C(x) = 2x^3 - 21x^2 + 60x + 500$, where x is the number of cookies made (in dozens), and $C(x)$ is the cost in dollars.

Determine where the graph of the equation is concave up and where it is concave down and find any *inflection* points.

(A) \longrightarrow The graph of the equation is concave down when $x < \frac{7}{2}$ and is concave up when $x > \frac{7}{2}$, and there is a point of *inflection* when $x = \frac{7}{2}$.

(B) \longrightarrow The graph of the equation is concave down for all values of x , and there is no point of *inflection*.

(C) \longrightarrow The graph of the equation is concave up for all values of x , and there is no point of *inflection*.

(D) \longrightarrow The graph of the equation is concave down when $x > \frac{7}{2}$ and is concave up when $x < \frac{7}{2}$, and there is a point of *inflection* when $x = \frac{7}{2}$.

(E) \longrightarrow None of the above statements is true.

=====

7Q7. If $f''(x) = x(x+1)(x-2)^2$, then the graph of f has *inflection* points when $x =$

(A) \longrightarrow -1 only

(B) \longrightarrow 2 only

(C) \longrightarrow -1 and 0 only

(D) \longrightarrow -1 and 2 only

(E) \longrightarrow $-1, 0,$ and 2 only

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8Q8. A rectangular plot adjacent to a stream is to be fenced in by using the stream as one side of the enclosed area.

If 2000 feet of fencing are to be used, find the maximum area that can be enclosed.

Assume the answer is in square feet.

(A) \longrightarrow 400000

(B) \longrightarrow 500000

(C) \longrightarrow 600000

(D) \longrightarrow 800000

(E) \longrightarrow 250000

9Q9. $\int_2^3 \frac{x dx}{x^2 + 1} =$

(A) $\longrightarrow \frac{1}{2} \ln \frac{3}{2}$

(B) $\longrightarrow \frac{1}{2} \ln 2$

(C) $\longrightarrow \ln 2$

(D) $\longrightarrow 2 \ln 2$

(E) $\longrightarrow \frac{1}{2} \ln 5$

10Q10. $\int_0^1 (x + 1) e^{x^2 + 2x} dx =$

(A) $\longrightarrow \frac{e^3}{2}$

(B) $\longrightarrow \frac{e^3 - 1}{2}$

(C) $\longrightarrow \frac{e^4 - e}{2}$

(D) $\longrightarrow e^3 - 1$

(E) $\longrightarrow e^4 - e$

11Q11. Given the function defined by $f(x) = 3x^5 - 20x^3$, find all values of x for which the graph of f is concave up.

(A) $\longrightarrow x > 0$

(B) $\longrightarrow -\sqrt{2} < x < 0$ or $x > \sqrt{2}$

(C) $\longrightarrow -2 < x < 0$ or $x > 2$

(D) $\longrightarrow x > \sqrt{2}$

(E) $\longrightarrow -2 < x < 2$

=====

12Q12. The number of bacteria in a culture is growing at a rate of $3000e^{\frac{2t}{5}}$ per unit of time.

At $t = 0$, the number of bacteria present was 7500.

Find the number present at $t = 5$.

(A) $\longrightarrow 1200e^2$

(B) $\longrightarrow 3000e^2$

(C) $\longrightarrow 7500e^2$

(D) $\longrightarrow 7500e^5$

(E) $\longrightarrow \frac{15000}{7}e^7$

=====

13Q13. What are all values of x for which the function f defined $f(x) = x^3 + 3x^2 - 9x + 7$ is increasing?

(A) $\longrightarrow -3 < x < 1$

(B) $\longrightarrow -1 < x < 1$

(C) $\longrightarrow x < -3$ or $x > 1$

(D) $\longrightarrow x < -1$ or $x > 3$

(E) \longrightarrow All real numbers.

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14Q14. The radius r of a sphere is increasing at the uniform rate of $\frac{dr}{dt} = 0.3$ inches per second.

At the instant when the surface area S becomes 100π square inches.

What is the rate of increase, in cubic inches per second, in the volume V ? $\frac{dV}{dt} =$

$\left(S = \text{Surface Area} = 4\pi r^2 \text{ and Volume} = V = \frac{4}{3}\pi r^3 \right).$

(A) $\longrightarrow 10 \pi$

(B) $\longrightarrow 12 \pi$

(C) $\longrightarrow 22.5 \pi$

(D) $\longrightarrow 25 \pi$

(E) $\longrightarrow 30 \pi$

=====

15Q15. The demand equation for a monopolist's product is $p = \frac{500}{\sqrt{q}}$, where p is the price per unit (in dollars) for q units. If the total cost c (in dollars) of producing q units is given by $c = 5q + 2000$, then the level of production at which profit is maximized is

[Hint : Revenue = $R = qp$; Profit = $P = R - c = \text{Revenue} - \text{Cost}$]

- (A) \longrightarrow 100 units
- (B) \longrightarrow 10000 units
- (C) \longrightarrow 900 units
- (D) \longrightarrow 1600 units
- (E) \longrightarrow 2500 units

=====

16Q16. The supply equation for a certain radio is given by $p = p(x) = 0.8\sqrt{x} + 17$ where p is the price in dollars and x is the number of radios supplied.

Use differentials only to approximate the price when 620 radios are supplied. (Hint : Use $x = 625$.)

[$p(x + dx) \approx p(x) + dp$; $dp = p'(x) dx$]

- (A) \longrightarrow approximately 36.92 dollars
- (B) \longrightarrow approximately 37.00 dollars
- (C) \longrightarrow approximately 37.08 dollars
- (D) \longrightarrow approximately 36.98 dollars
- (E) \longrightarrow approximately 36.84 dollars

=====

17Q17. The exact area of the region bounded by the graphs of $y = x^2 + x + 1$, $x = -2$, $x = 1$, and the $x - axis$ is

(A) $\longrightarrow \frac{5}{2}$ square units

(B) $\longrightarrow \frac{7}{2}$ square units

(C) $\longrightarrow \frac{9}{2}$ square units

(D) $\longrightarrow \frac{11}{2}$ square units

(E) $\longrightarrow \frac{13}{2}$ square units

=====

18Q18. The exact area of the region bounded by the graphs of $y = x^2 - 5$ and $y = 2x + 3$ is

(A) $\longrightarrow \frac{9}{2}$ square units

(B) $\longrightarrow 36$ square units

(C) $\longrightarrow 60$ square units

(D) $\longrightarrow 24$ square units

(E) $\longrightarrow \frac{73}{3}$ square units

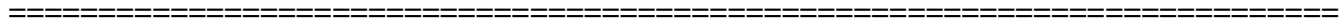
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19Q19. Find all the horizontal and vertical asymptotes of the following function $f(x)$.

$$f(x) = \frac{x^2}{x^2 + 2x - 5}.$$

Then which one of the following statements is true.

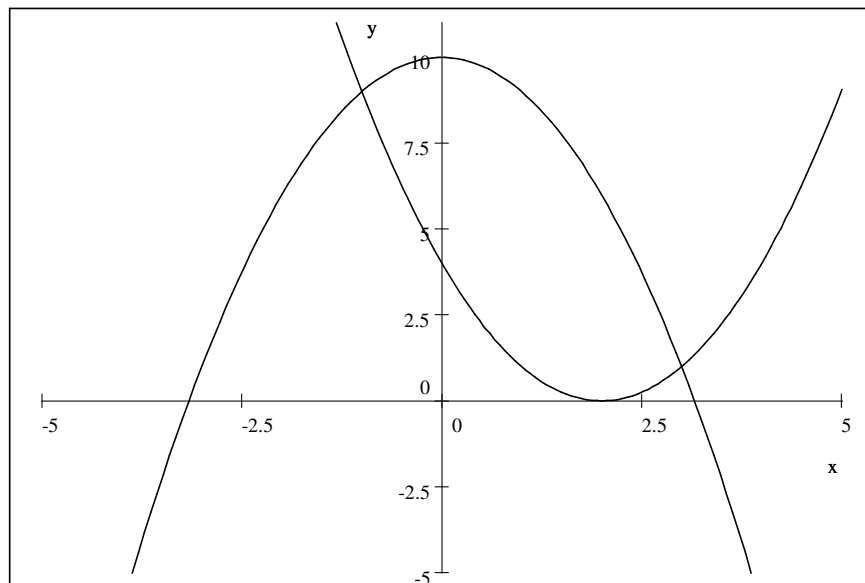
- (A) Exactly one horizontal asymptote and exactly one vertical asymptote.
- (B) No horizontal asymptote and no vertical asymptote.
- (C) Exactly one horizontal asymptote and exactly two vertical asymptotes.
- (D) Exactly two horizontal asymptotes and exactly one vertical asymptote.
- (E) Exactly two horizontal asymptotes and exactly two vertical asymptote.



20Q20. Find the area of the region that is between the curves

$$y = x^2 - 4x + 4 \text{ and } y = 10 - x^2$$

from $x = 2$ to $x = 4$.



(A) \rightarrow 4

(B) \rightarrow 8

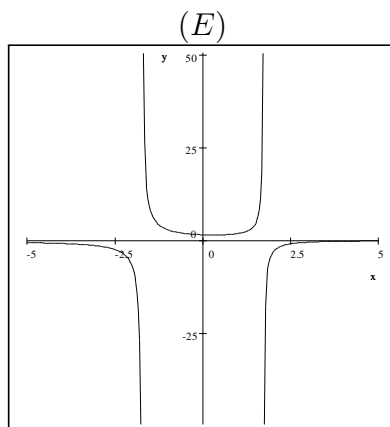
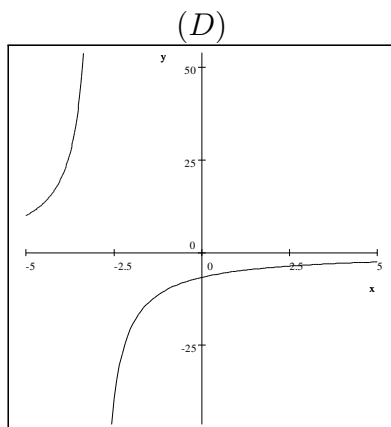
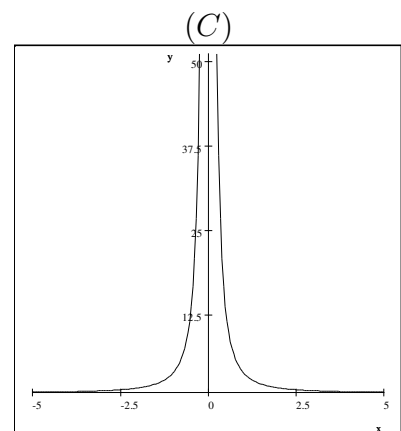
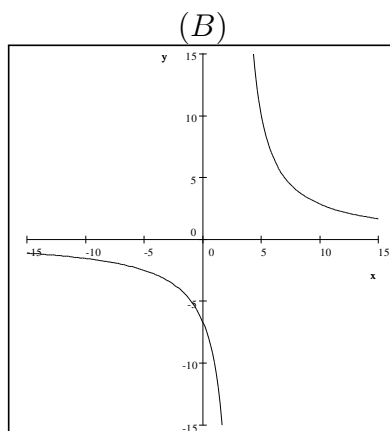
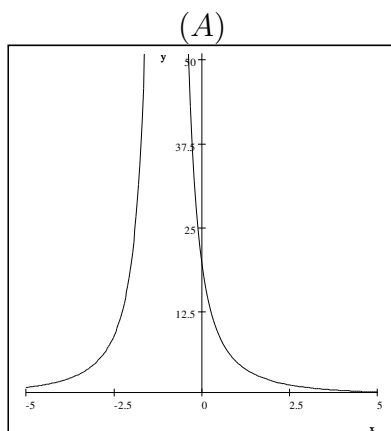
(C) \rightarrow 12

(D) \rightarrow 16

(E) \rightarrow 6

21Q21. A released film has a revenue given by $y(x) = \frac{20}{x+3}$, where $y(x)$ is in millions of dollars and x is the number of weeks after its release.

Sketch the graph of this function.



MATH-132-093-EXAM-II

Qn#	A	B	C	D	E	Letter
1	√					A
2			√			C
3	√					A
4			√			C
5					√	E
6	√					A
7			√			C
8		√				B
9		√				B
10		√				B
11		√				B
12			√			C
13			√			C
14					√	E
15					√	E
16	√					A
17			√			C
18		√				B
19			√			C
20		√				B
21	√					A
Sum						126