

Full Name:
Section:

ID:

Question 1 Determine whether the following series are convergent or divergent.
Justify your answer.

$$a) \sum_{n=1}^{\infty} \sin\left(\frac{n\pi}{2}\right) \ln\left(1 + \frac{1}{n}\right), \quad b) \sum_{n=2}^{\infty} \frac{\cos\left(\frac{1}{n}\right)}{n\sqrt{n} + \cos(n)}, \quad c) \sum_{n=1}^{\infty} \frac{\ln(n!)}{n^3}$$
$$d) \sum_{n=1}^{\infty} \left(\frac{n}{n+1}\right)^{2n}, \quad e) \sum_{n=0}^{\infty} \frac{(1.5.9 \dots (4n+1))^3}{n!(2n)!3^{2n}}.$$

Question 2 For which values of p , the series $\sum_{n=2}^{\infty} \frac{1}{n(\ln n)^p}$ is convergent.

Question 3 Let $S = \sum_{n=0}^{\infty} \frac{(-1)^n}{n^3+1}$ and let S_n be the partial sum of the first n terms. Find the minimum value of n such that $|S - S_n| < 0.001$.