

Full Name:
Section:

ID:

Question 1 Determine whether the following series are convergent or divergent.
Justify your answer.

$$a) \sum_{n=2}^{\infty} \frac{1}{n(\sqrt{\ln n})}, \quad b) \sum_{n=3}^{\infty} \cos(\pi/n) \left(\frac{n+1}{n}\right)^n, \quad c) \sum_{n=1}^{\infty} \sin\left(\frac{(-1)^n}{n}\right).$$

Question 2 Find the interval of convergence of the power series $\sum_{n=1}^{\infty} \frac{(2x+e)^n}{ne^n}$.

Question 3 Find the sum of the following series if possible. Justify your answer.

$$a) \sum_{n=2}^{\infty} 5^{1-n} 2^{2n+1} \quad b) \sum_{n=1}^{\infty} \ln \left(1 - \frac{2}{2n+1} \right).$$

Question 4 Let $S = \sum_{n=5}^{\infty} \frac{(-1)^n}{\sqrt[3]{n}}$ and let S_n be the partial sum of the first n terms. Find the minimum (integer) value of n such that $|S - S_n| < 0.1$.