

Write clearly, explain and simplify your answers

1. [6pts] Use logarithmic differentiation to find y' if $y = x^{x^4}$

2. [6pts] Find $y''(-1)$ if $y = (x^2 - 3x + 1)^2$

3. [6pts] The demand equation for a product is given by $3p + 2q = 300$, where p is the unit price when q units are produced. How many units should be produced to maximize revenue and what is the value of this maximum revenue?

4. [12pts] For the function $f(x) = 2x^3 - 9x^2 + 12x + 7$ determine
- (a) the intervals where it is increasing and where it is decreasing
 - (b) each relative maximum and relative minimum
 - (c) the intervals where it is concave up and where it is concave down
 - (d) the x -coordinate of each inflection point

5. [6pts] Using differentials, find an approximation of $\sqrt[5]{30}$

6. [8pts] The cost function c of producing q units of a product is $c = 0.05q^2 + 5q + 500$, where $50 \leq q \leq 200$. How many units should be produced to minimize the average cost per unit?

7. [8pts] Evaluate:

(a) $\int x^2 4^{5x^3+7} dx$

(b) $\int_0^1 (4x - 6)(3x - x^2)^4 dx$

8. [8pts] Evaluate:

(a) $\int \frac{3x^2 - 4x + \sqrt{x}}{x^3} dx$

(b) $\int \frac{x^2 - 3x + 4}{x - 2} dx$