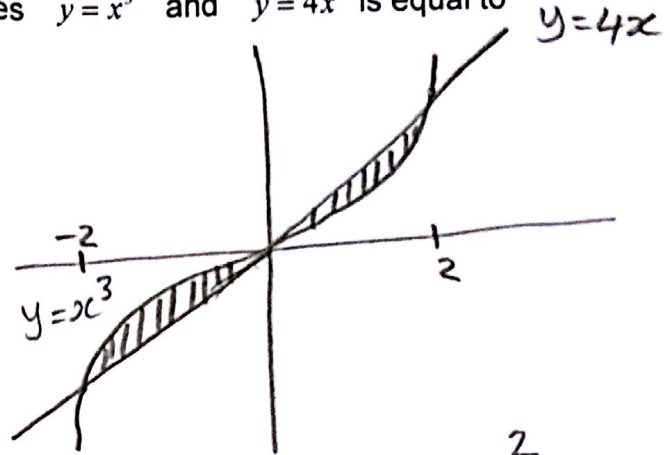


(show all your work and circle one letter to get a full mark or you will get zero)

1) The area of the region lying between the curves  $y = x^3$  and  $y = 4x$  is equal to

- (a)  $\int_{-2}^0 (4x - x^3) dx + \int_0^2 (x^3 - 4x) dx$   
 (b)  $-2 \int_0^2 (4x - x^3) dx$   
 (c)  $\int_{-2}^2 (x^3 - 4x) dx$   
 (d)  $\int_{-2}^2 (x^3 - 4x) dx - \int_0^2 (4x - x^3) dx$   
 (e)  $\int_{-2}^0 (x^3 - 4x) dx + \int_0^2 (4x - x^3) dx$   
 (f) none of the above



intersection points

$$x^3 = 4x \Rightarrow x^3 - 4x = 0$$

$$\rightarrow x(x^2 - 4) = 0 \Rightarrow$$

$$x = -2, 0, 2$$

$$\text{Area} = \int_{-2}^0 (x^3 - 4x) dx + \int_0^2 (4x - x^3) dx$$

2)  $\int_0^{\sqrt{e-1}} \frac{2t}{t^2+1} \ln(t^2+1) dt = I$

(a)  $\frac{3}{2}$

(b)  $\frac{1}{2}$

(c)  $\frac{e}{2}$

(d)  $\frac{3e}{4}$

(e)  $\frac{1}{2}(e-1)$

(f) none of the above

Let  $u = \ln(t^2+1) \rightarrow du = \frac{2t}{t^2+1} dt$

$$\Rightarrow \int \frac{2t}{t^2+1} \ln(t^2+1) dt = \int u du$$

$$= \frac{1}{2} u^2 + c = \frac{1}{2} [\ln(t^2+1)]^2 + c$$

Now,  $I = \left[ \frac{1}{2} [\ln(t^2+1)]^2 \right]_0^{\sqrt{e-1}}$

$$= \frac{1}{2} [\ln(e-1+1)]^2 - \frac{1}{2} [\ln(1)]^2$$

$$= \frac{1}{2} - 0 = \frac{1}{2}$$

3) The area of the region enclosed by the curves  $y = 4 - x^2$ ,  $y = 2x - 4$  and  $y = 4$  is equal to

(a)  $\int_0^4 ((4x - x^2) - (2x - 4)) dx$

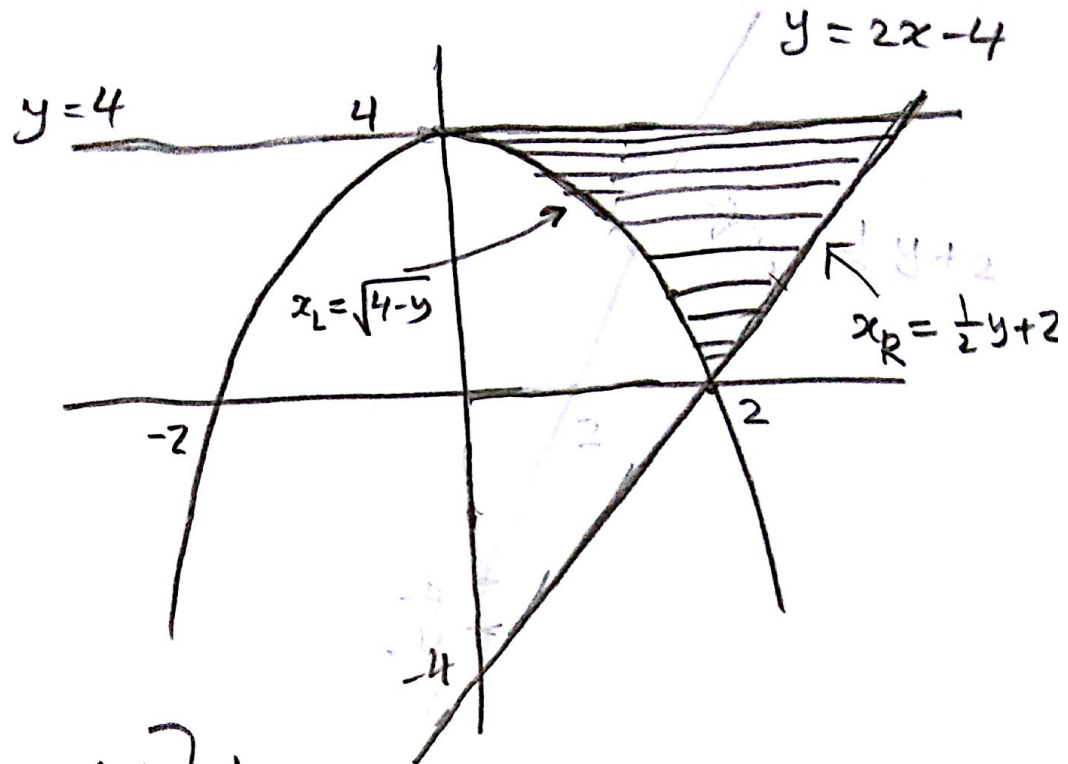
(b)  $\int_2^4 ((\frac{1}{2}y + 2) - (\sqrt{4 - y})) dy$

(c)  $\int_0^4 ((\frac{1}{2}y + 2) - (-\sqrt{4 - y})) dy$

(d)  $\int_0^4 ((\frac{1}{2}y + 2) - (\sqrt{4 - y})) dy$

(e)  $\int_0^2 ((2x - 4) - (4 - x^2)) dx$

(f) none of the above



$$\text{Area} = \int_{y=0}^{y=4} [x_R(y) - x_L(y)] dy$$

$$= \int_0^4 \left[ \left(\frac{1}{2}y + 2\right) - (\sqrt{4 - y}) \right] dy$$