

Serial No.: \_\_\_\_\_ Student Name: \_\_\_\_\_ Student Number: \_\_\_\_\_

Instructor: M. Z. Abu-Sbeih

Math 101- Q1

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**Problem 1: (6 points)** Find the average rate of the function  $y = x^2 - x$  with respect to  $x$  over the interval  $[1, 1+h]$ . What will happen when  $h$  approaches 0? What is the slope of the tangent line to the curve at that point  $(1,0)$ ?

**Problem 2: (18 points)**

(i) Use the precise definition of the limit to show that  $\lim_{x \rightarrow 2} (2 - 3x) = -4$ .

If  $\epsilon = 0.06$ , find the largest corresponding  $\delta > 0$  which satisfies the definition.

(ii) For the limit  $\lim_{x \rightarrow 3} \sqrt{x-2} = 1$ , find a  $\delta > 0$  that works for  $\epsilon = 1$  in the definition of the limit.

(iii) If  $\lim_{x \rightarrow 1} \frac{2+x-f(x)}{x-1} = 5$ , find  $\lim_{x \rightarrow 1} f(x)$ . Justify your answer.

**Problem 3: (18 points)** Find the limit if it exists

a)  $\lim_{x \rightarrow 3} \frac{x+3}{x^2+x-6}$

b)  $\lim_{x \rightarrow 4} \frac{4x-x^2}{2-\sqrt{x}}$

c)  $\lim_{x \rightarrow 1} (1-x)^2 \cos \frac{6}{1-x^2}$  (Use the sandwich Theorem)