

King Fahd University of Petroleum and Minerals  
Department of Mathematics and Statistics  
Math 101 (142) Sec 15 - Quiz 5

Name:

ID:

Serial No.:

1. Find a constant  $c$  that satisfies the conclusion of the mean value theorem when applied to  $f(x) = x^4 - x$  on  $[-1, 1]$

2. Suppose that  $f$  is differentiable on  $\mathbb{R}$  and satisfies  $2 \leq f'(x) \leq 6$  for all values of  $x$ . Then find  $a$  and  $b$ , where  $a \leq f(5) - f(3) \leq b$

3. Find the critical point(s) of  $f(x) = \frac{x^2 + 3}{\sqrt{2x + 1}}$

4. Find the absolute maximum and minimum of  $f(x) = \cos^2 x - \cos x$ ,  $-\frac{\pi}{2} \leq x \leq \pi$

5. If the function  $f(x) = axe^{bx^2}$  has the maximum value  $f(2) = 1$  where  $a$  and  $b$  are real numbers, then find  $a$  and  $b$