

Full Name:

ID:

Section and Serial number:

Question 1 Find the inverse of the given matrix

$$A = \begin{bmatrix} 1 & -1 & 3 \\ 6 & 4 & -3 \\ 2 & 3 & -4 \end{bmatrix}$$

Question 2 Given that A and B are two square matrices of the same size. If $|A| = 2$ and $|B| = 3$ then find $|(A^{-1}B)^T A^3 B^2|$.

Question 3 a) Show that the following system has a unique solution:

$$\begin{cases} -2x + 2y - z + 2t = 0 \\ 2x + y + 2z - 3t = 0 \\ x - y - z + t = 1 \\ 3x - 3y + z - t = 0 \end{cases}$$

b) Find t only.

Question 4 Let $V = \mathbb{R}^3$. For any $a = (x, y, z) \in V$ and any $\alpha \in \mathbb{R}$, the multiplicative operator is given by:

$$\alpha \cdot a = (\alpha x, 1, \alpha z).$$

Show that $(V, +, \cdot)$ is not a vector space over \mathbb{R} .