

**Problem 1:** (18 points) Find the limit if it exists. If it does not exist, show why. Use the symbols  $\infty$  or  $-\infty$  as appropriate.

(i)  $\lim_{x \rightarrow 3} \frac{x^2 - 2x - 3}{x^2 + 2x - 15}$

(ii)  $\lim_{x \rightarrow 6} \frac{\sqrt{x-2} - 2}{x-6}$

(iii)  $\lim_{x \rightarrow -\infty} \frac{3 - 2x - 2x^3}{7 - 5x^3 + 2x^2}$

**Problem 2:** (22 points)

(a) Find all values of  $A$  which will make the following function continuous.

$$f(x) = \begin{cases} 1 - Ax^2 & \text{if } x \leq 2, \\ 2A - x & \text{if } x > 2. \end{cases}$$

(b) Find all points of discontinuity of the function  $f(x) = \frac{x-1}{x^2-1}$  if any exists and state the type of each one.

(c) If  $f(x) = x^2 - x$ , find  $\lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$