

Full Name:

ID:

Serial number:

Question 1. (a) Use two rectangles and midpoints to approximate the area under the curve $y = 1 + \sin(x) \sin(2x)$ for $0 \leq x \leq \pi$. (b) Evaluate the area.

Question 2. A particle moves along a line so that its velocity at time t is $v(t) = -t(1 - 2t)^7$. Find the displacement by the particle during the time period $0 \leq t \leq 1$.

Question 3. Evaluate

a) $\lim_{n \rightarrow \infty} \frac{1}{n} \sum_{i=1}^n 3^{1+\frac{i}{2n}}$

b) $\int \frac{1}{3e^x + e^{-x}} dx$

Question 4. If

$$f(x) + \int_{2x-1}^{3-x} e^{t^2} dt = 3x.$$

Find $f''(1)$.

Question 5. Evaluate (you may interpret the integral as an area)

$$\int_{-1}^3 \sqrt{3 - x^2 + 2x} dx$$