

SHOW ALL YOUR WORK. NO CREDITS FOR ANSWERS WITHOUT JUSTIFICATIONS

(1) (22 points) Find the limit if it exists

a) $\lim_{x \rightarrow 3^-} \frac{x^2 - 3x}{x^2 - 6x + 9}$

b) $\lim_{x \rightarrow 2} \frac{\sqrt{x^2 + 5} - 3}{x - 2}$

c) $\lim_{x \rightarrow 0} \left(3 + x^2 e^{\cos \frac{1}{x}} \right)$

d) $\lim_{x \rightarrow 0^+} \left(\frac{1}{x} - \ln x \right)$

Problem 2: (6 points) Is the function $f(x) = [x] + [-x]$ continuous at $x = 2$? If not what is the type of discontinuity? (Show all your work).

Problem 3: (6 points) Use the $\epsilon - \delta$ definition of limit to show that $\lim_{x \rightarrow 2} (3 - 2x) = -1$.

Find values of δ that correspond to $\epsilon = 0.06$

Problem 5: (6 points) Consider the function $f(x) = \frac{x^2 - 1}{x^2 - 3x - 4}$.

(a) Find all values of x where the function is discontinuous and state the type of each one.

(b) Find all vertical asymptotes of the function.