

King Fahd University of Petroleum and Minerals
Math. & Stat. Department
QUIZ # 2

Name	ID	SEC 15	Sr#
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Q1) (5 pts) For what value of k the function $f(x)$ has a removable discontinuity at $x = 0$?

$$f(x) = \begin{cases} k - \sin x & , x < 0 \\ 1 & , x = 0 \\ x^2 - k^2 + 2, & x > 0 \end{cases}$$

Q2)(5 pts) If $f(x) = x^2 + 10 \sin x$, show that there is a number c such that $f(c) = 1000$.

Q3) (5 pts) Find all vertical and horizontal asymptotes of $f(x) = \arctan\left(\frac{\sqrt{9x^2+2}}{3x+7}\right)$. Justify your answer by using limits.

Q4)(5 pts) Find the equation of the tangent line to the curve $f(x) = \sqrt{1-2x}$ at $x = -4$.

Q5) (4 pts bonus) Suppose $f(x)$ is a differentiable function that satisfies the following

$f(x+y) = f(x) + f(y) + 2xy - 1$ for any real numbers x and y and $\lim_{x \rightarrow 0} \frac{f(x)-1}{x} = -2$.

Then find $\hat{f}(1)$.