

Math102 Term182  
Sec 2 Quiz 1

Name	ID	Sr
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**Instruction: CIRCLE one answer and SHOW all your work to get full mark**

Q1) The limit

$$\lim_{n \rightarrow \infty} \sum_{i=1}^n \frac{\pi}{4n} \sin^2 \left( \frac{\pi i}{4n} + \frac{\pi}{3} \right)$$

can be interpreted as the area under the curve

a)  $y = \sin^2(x + \frac{\pi}{3})$  on  $[0, \frac{\pi}{3}]$

b)  $y = \sin^2(x^2)$  on  $[\frac{\pi}{4}, \frac{\pi}{3}]$

c)  $y = \sin(x^2)$  on  $[0, \frac{\pi}{3}]$

d)  $y = \sin(x^2)$  on  $[0, \frac{\pi}{4}]$

e)  $y = \sin^2(x)$  on  $[\frac{\pi}{3}, \frac{7\pi}{12}]$

Q2) If  $R_n$  is the Riemann sum for  $f(x) = x^2 + 2x$ ,  $1 \leq x \leq 4$ , with  $n$  subintervals and taking the sample points to be the right endpoints, then  $R_n =$

a)  $9 + 18 \frac{n+1}{n} + \frac{9(n+1)(2n+1)}{2n^2}$

b)  $9 + 9 \frac{n+1}{n} + \frac{9(n+1)(2n+1)}{2n^2}$

c)  $20 \frac{n+1}{n} + \frac{16(n+1)(2n+1)}{2n^2}$

d)  $18 \frac{n+1}{n} + \frac{9(n+1)(2n+1)}{n^2}$

e)  $18 + \frac{9(n+1)(2n+1)}{2n^2}$

Q3) Using the comparison properties of the integrals (Property 8) to estimate  $I = \int_0^\pi \sqrt{2 + \sin x}$ , we get :

a)  $\sqrt{2} \leq I \leq \sqrt{3}$

b)  $0 \leq I \leq \sqrt{2}$

c)  $-\sqrt{3} \leq I \leq -\sqrt{2}$

d)  $\pi\sqrt{2} \leq I \leq \pi\sqrt{3}$

e)  $\frac{\pi}{2} \leq I \leq \pi$

Q4) If  $F(x) = \int_1^x f(t)dt$  and  $f(t) = \int_1^{t^2} \sin(1 + u^2)du$ , then  $F''(1) =$

a)  $\sin(1)$

b)  $\sin(2)$

c)  $2\sin(2)$

d)  $4\sin(2)$

e)  $2\sin(2) \cos(2)$

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Sec5 Quiz 1

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**Instruction: CIRCLE one answer and SHOW all your work to get full mark**  
Q1) Using **three rectangles and left endpoints**, the approximation of the area under the graph of  $f(x) = \frac{1}{x+1}$  from  $x = 1$  to  $x = 3$  is equal to:

a)  $\frac{33}{25}$

b)  $\frac{27}{20}$

c)  $\frac{49}{50}$

d)  $\frac{25}{38}$

e)  $\frac{47}{60}$

Q2) If  $R_n$  is the Riemann sum for  $f(x) = x^2 + 2x$ ,  $1 \leq x \leq 3$ , with  $n$  subintervals and taking the sample points to be the right endpoints, then  $R_n =$

a)  $6 + \frac{8(n+1)}{n} + \frac{2(n+1)(2n+1)}{3n^2}$

b)  $15 - \frac{(n+1)}{n} + \frac{4(n+1)(2n+1)}{3n^2}$

c)  $\frac{20(n+1)}{n} + \frac{4(n+1)(2n+1)}{3n^2}$

d)  $4 + \frac{10(n+1)}{n} + \frac{4(n+1)(2n+1)}{3n^2}$

e)  $6 + \frac{8(n+1)}{n} + \frac{4(n+1)(2n+1)}{3n^2}$

Q3)

$$\lim_{n \rightarrow \infty} \sum_{i=1}^n \frac{2\pi}{n} \tan^{-1} \left( 2\pi + \frac{\pi i}{n} \right) =$$

a)  $\int_{2\pi}^{3\pi} 2 \tan^{-1}(x) dx$

b)  $\int_0^{\pi} \tan^{-1}(x + \pi) dx$

c)  $\int_{\pi}^{2\pi} \tan^{-1}(x + 3\pi) dx$

d)  $\int_{\pi}^{2\pi} 2 \tan^{-1}(x + 5\pi) dx$

e)  $\int_{2\pi}^{3\pi} \tan^{-1}(x) dx$

Q4) If  $g$  is a continuous function such that

$$\int_{\pi}^x e^{-t} g(t) dt = \pi^2 + x \sin x \text{ for all } x, \text{ then } g(x)$$

a)  $x e^x \sin x$

b)  $e^x \cos x$

c)  $e^x (2\pi + x \cos x + \sin x)$

d)  $e^x (x \cos x + \sin x)$

e)  $e^x \cos x$

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Sec 19 Quiz 1

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**Instruction: CIRCLE one answer and SHOW all your work to get full mark**

Q1) Using **three rectangles and midpoints**, the approximation of the area under the graph of  $f(x) = \frac{x}{x-1}$  from  $x = 2$  to  $x = 8$  is equal to:

a)  $\frac{29}{3}$

b)  $\frac{41}{12}$

c)  $\frac{47}{12}$

d)  $\frac{136}{15}$

e)  $\frac{47}{6}$

Q2) If  $R_n$  is the Riemann sum for  $f(x) = x^2 + 2x$ ,  $1 \leq x \leq 3$ , with  $n$  subintervals and taking the sample points to be the right endpoints, then  $R_n =$

a)  $\frac{8(n+1)}{n} + \frac{4(n+1)(2n+1)}{3n^2}$

b)  $10 + \frac{20(n+1)}{3n}$

c)  $-\frac{n+1}{2n} - \frac{(n+1)(2n+1)}{6n^2}$

d)  $4 + \frac{10(n+1)}{n} + \frac{4(n+1)(2n+1)}{3n^2}$

e)  $6 + \frac{8(n+1)}{n} + \frac{4(n+1)(2n+1)}{3n^2}$

Q3)

$$\lim_{n \rightarrow \infty} \sum_{i=1}^n \frac{6}{n} \ln \left( 2 + \frac{3i}{n} \right) =$$

a)  $\int_2^5 \ln(x) dx$

b)  $\int_2^5 2\ln(x) dx$

c)  $\int_0^3 \ln(1+x) dx$

d)  $\int_1^4 \ln(2+x) dx$

e)  $\int_1^4 \ln(6+x) dx$

Q4) If  $g$  is a continuous function such that

$$\int_{\pi}^{2x+1} e^{t/2} g(t) dt = xe^x, \text{ then } g(7)$$

a)  $\frac{2}{\sqrt{e}}$

b)  $\frac{4}{\sqrt{e}}$

c)  $4e^{-8}$

d)  $8e^{-8}$

e)  $\frac{7}{2e^8}$

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Sec24 Quiz 1

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**Instruction: CIRCLE one answer and SHOW all your work to get full mark**

Q1) The limit

$$\lim_{n \rightarrow \infty} \sum_{i=1}^n \frac{5}{n} \left( \frac{5i}{n} + 3 \right)^4$$

can be interpreted as the area under the curve

- a)  $y = x^4$  on  $[0,5]$
- b)  $y = x^4$  on  $[5,10]$
- c)  $y = x^4$  on  $[3,8]$**
- d)  $y = \frac{x^5}{5}$  on  $[0,5]$
- e)  $y = (x + 5)^4$  on  $[0,5]$

Q2) If  $R_n$  is the Riemann sum for  $f(x) = x^2 - 2x$ ,  $1 \leq x \leq 4$ , with  $n$  subintervals and taking the sample points to be the right endpoints, then  $R_n =$

- a)  $1 + \frac{2(n+1)}{n} + \frac{3(n+1)(2n+1)}{2n^2}$
- b)  $-3 + \frac{9(n+1)(2n+1)}{6n^2}$
- c)  $\frac{n+1}{n} + \frac{5(n+1)(2n+1)}{2n^2}$
- d)  $-3 + \frac{9(n+1)(2n+1)}{2n^2}$**
- e)  $-6 + \frac{9(n+1)(2n+1)}{2n^2}$

Q3) Using the comparison properties of the integrals (Property 8) to estimate  $I = \int_{-2}^0 x e^x$ , we get :

a)  $0 \leq I \leq \frac{2}{e^2}$

b)  $-\frac{4}{e^2} \leq I \leq 0$

c)  $-\frac{1}{e} \leq I \leq 1$

d)  $-\frac{2}{e^2} \leq I \leq 0$

e)  $-\frac{2}{e} \leq I \leq 0$

Q4) If

$$f(x) = \int_{\sin x}^{\cos(3x)} \frac{1}{\sqrt{1+4t^2}} dt,$$

then  $f'(\frac{\pi}{2}) =$

a) 3

b)  $\frac{3}{5}$

c)  $-\frac{14}{5}$

d)  $\frac{16}{5}$

e) 2