## MATH 555 COMMUTATIVE ALGEBRA

## 1. DESCRIPTION

Basics of rings and ideals. Rings of fractions, integral dependence, valuation rings, discrete valuation rings, Dedekind domains, fractional ideals. Topologies and completions, filtrations, graded rings and modules. Dimension theory.

## **2.** Техтвоок

M. F. Atiyah & I. G. Macdonald, INTRODUCTION TO COMMUTATIVE ALGEBRA, Addison-Wesley, **1969**. Paperback edition, Perseus Publishing, December **1994**.

WEEK	MATERIAL
1	1. RINGS & IDEALS.
	Exercises & problems.
2	2. Rings and Modules of Fractions.
	Exercises & problems.
3	3. Integral Dependence and Valuations. Integral dependence.
	Cohen-Seidenberg [going-up & going-down] theorems.
4	Valuation rings.
	Hilbert's Nullstellensatz.
5	Noether's normalization lemma.
	Exercises & problems.
6	4. NOETHERIAN RINGS. ARTINIAN RINGS.
	Exercises & problems.
7	5. DISCRETE VALUATION RINGS AND DEDEKIND DOMAINS. Discrete valuation rings.
	Dedekind domains
8	Structure theorems [via fractional ideals].
	Exercises & problems.
9	6. COMPLETIONS. Topologies & Completions.
10	Graded rings and modules.
11	The associated graded ring.
	Exercises & problems.
12	7. DIMENSION THEORY. Hilbert functions
13	Dimension theorem for Noetherian local rings.
14	Regular local rings.
	Local dimension theorem for irreducible affine varieties.
15	Exercises & problems.

## 3. Syllabus

# 4. GRADING POLICY

Take-home Exam 1	Chapters 1-3	120
Take-home Exam 2	Chapters 4-7	180
Research Project	-	100