

**King Fahd University of Petroleum and Minerals**  
**Department of Mathematics & Statistics**

**MATH 566 Syllabus (Semester I, 201)**  
**Dr. N. Tatar**

**Course Title:** Fractional Differential Equations

**Course Description:**

Special functions (Gamma, Mittag-Leffler, and wright), Riemann fractional integral, Riemann-Liouville and Caputo fractional derivatives, composition rules, embeddings, equivalence with integral equations, well posedness for Cauchy type problems, successive approximation method, Laplace and Mellin transform methods

**Textbook:**

A. A. Kilbas, H. M. Srivastava and J. J. Trujillo, "Theory and Applications of Fractional Differential Equations", 2006

**Other references:**

Igor Podlubny, Fractional Differential Equations, Vol. 198 in Mathematics and Science and Engineering, Academic Press, 1999.

S. G. Samko, A. A. Kilbas and O.I. Marichev, Fractional Integrals and Derivatives: Theory and Applications, Gordon and Breach Science Publishers, 1993

**Learning Outcomes:**

- Use the properties of the Gamma function and Mittag-Leffler functions
- Use the properties of fractional integrals and fractional derivatives
- State the well-posedness for some fractional differential problems
- Describe the appropriate underlying spaces
- Link FDE's to their corresponding Volterra integral equations
- Use transforms to solve linear fractional differential equations

**Grading:**

Assessment 1:	15%
Midterm Exam:	15%
Assessment 3:	15%
Homework Assignments:	15%
Presentations:	15%
Final Exam:	25%

## Week Sections Material

<b>Week</b>	<b>Sections</b>	<b>Material</b>
<b>1</b>		Overview
<b>2</b>	<b>1.1</b> <b>1.4</b> <b>1.5</b> <b>1.8</b> <b>1.10</b>	Preliminaries: Spaces of continuous functions, special functions, transforms
<b>3</b>		The Abel integral equation (solvability in L1)
<b>4-5</b>	<b>2.1</b>	Riemann-Liouville fractional integral and fractional derivative
<b>6-7</b>	<b>2.4</b>	Caputo fractional derivative Grunwald fractional derivative
<b>8-9</b>	<b>3.3.1</b> <b>3.3.2</b> <b>3.3.3</b> <b>3.3.5</b>	Fractional differential problems with RL derivative
<b>10-11</b>	<b>3.5.1</b> <b>3.5.3</b>	Fractional differential problems with Caputo derivative
<b>12-13</b>	<b>4.1.1</b> <b>4.1.2</b> <b>4.1.3</b>	Explicit solving of FDEs
<b>14-15</b>	<b>5.3.1</b> <b>5.3.2</b>	Laplace transform